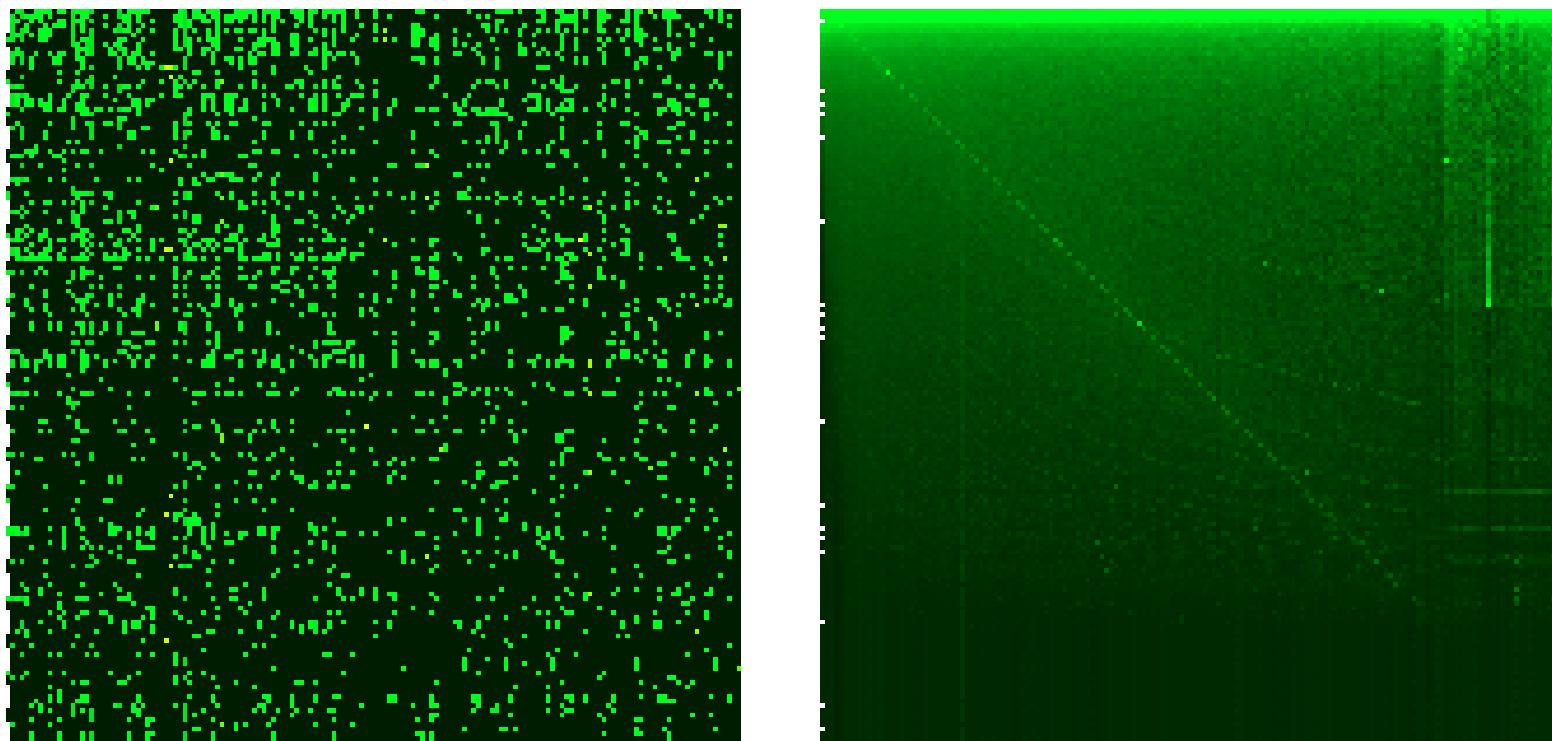


ApliGoogle

Applications of Google matrix to directed networks and Big Data

Colloque de restitution du Défi MASTODONS CNRS 2016



Google matrix G of the English Wikipedia network (Aug. '09) $N=3\,282\,257$. Left panel : close up 200×200 first elements.

<http://www.quantware.ups-tlse.fr/APLIGOOGLE/>

ApliGoogle partners



ApliGoogle « Kick-off » meeting, Luchon, May 16th 2016

ApliGoogle partners



**Laboratoire de Physique Théorique
de Toulouse (UMR CNRS 5152)**

- **DR1 D. Shepelyansky (PI)**
- Pr. K. Frahm

Expertises: Quantum chaos,
Random Matrix Theory, Complex
directed networks



<http://www.quantware.ups-tlse.fr/dima>

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- MCF K. Jaffrès-Runser
- Samer El Zant (doctorant)
- Dr. T. Peng (post-doctorant)

Expertises: Wireless networks



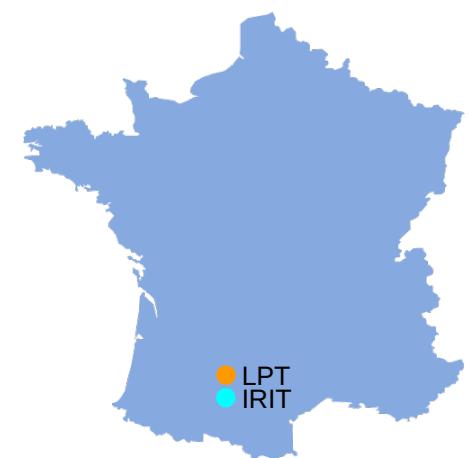
<http://www.irit.fr/~Katia.Jaffres>



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Institut Curie (INSERM U900)

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- Dr. I. Kuperstein
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- U. Czerwinska (doctorante)

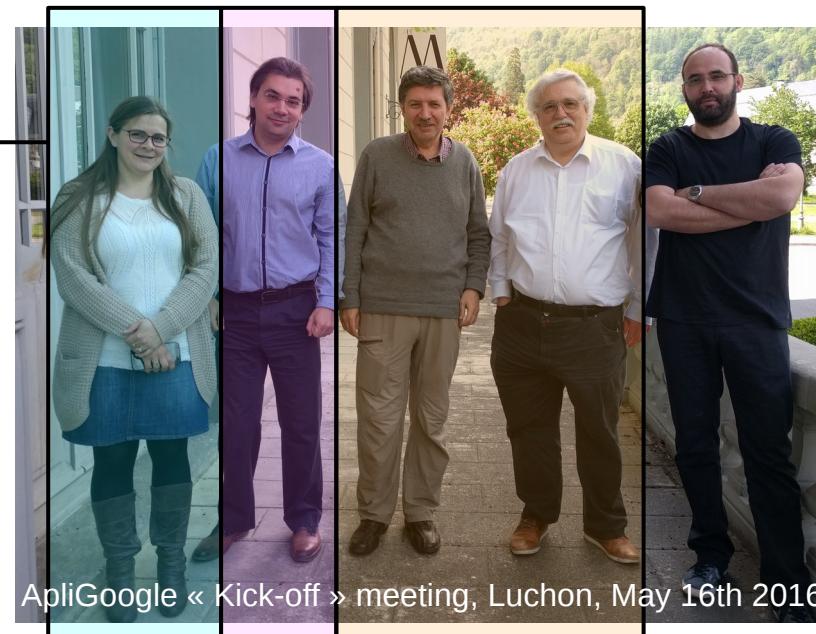
Expertises: Computational Biology, Systems Biology of Cancer



<http://www.ihes.fr/~zinovyev/>

ApliGoogle

Applications of Google matrix to directed networks and Big Data



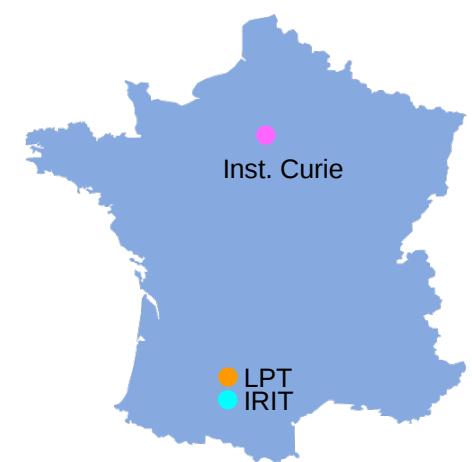
Laboratoire de Physique Théorique de Toulouse (UMR CNRS 5152)

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Expertises: Quantum Random Matrix Theory, chaos, Complex directed networks



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ApliGoogle

Applications of Google matrix to directed networks and Big Data



Institut UTINAM (UMR CNRS 6213)

- MCF J. Lages
- S. Diakité (ingénieur)
- F. Gazelle (ingénieur)

Expertises: Quantum chaos, Random Matrix Theory, Complex directed networks



<http://perso.utinam.cnrs.fr/~lages>

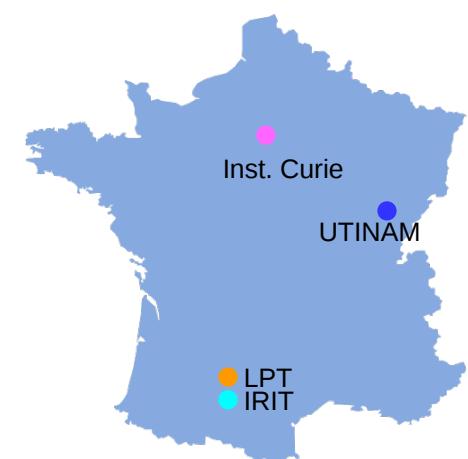
Laboratoire de Physique Théorique de Toulouse (UMR CNRS 5152)

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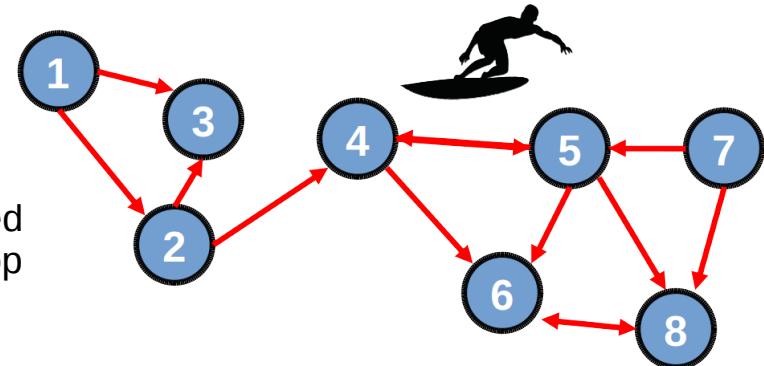
<http://www.quantware.ups-tlse.fr/dima>



How Google works

From Markov (1906) to Brin & Page (1998)

Markovian process : a random surfer probe the structure of a directed network. At each step, the surfer choose randomly an adjacent node to hop and continue its journey.



Adjacency matrix

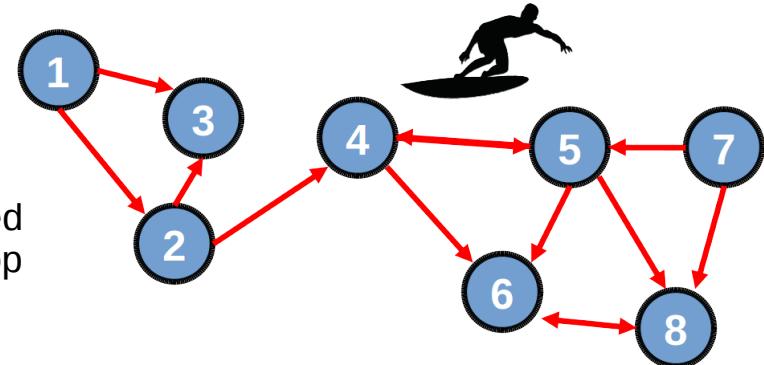
$$A_{ij} = \begin{cases} 0 & \text{si } j \rightarrow i \\ 1 & \text{si } j \not\rightarrow i \end{cases}$$

$$\mathbf{A} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 1 & 1 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 & 1 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 1 & 1 & 0 \end{pmatrix}$$

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Adjacency matrix

$$A_{ij} = \begin{cases} 0 & \text{si } j \rightarrow i \\ 1 & \text{si } j \not\rightarrow i \end{cases} \quad S_{ij} = \begin{cases} A_{ij} / \sum_{k=1}^N A_{kj} & \text{si } \sum_{k=1}^N A_{kj} \neq 0 \\ 1/N & \text{sinon} \end{cases}$$

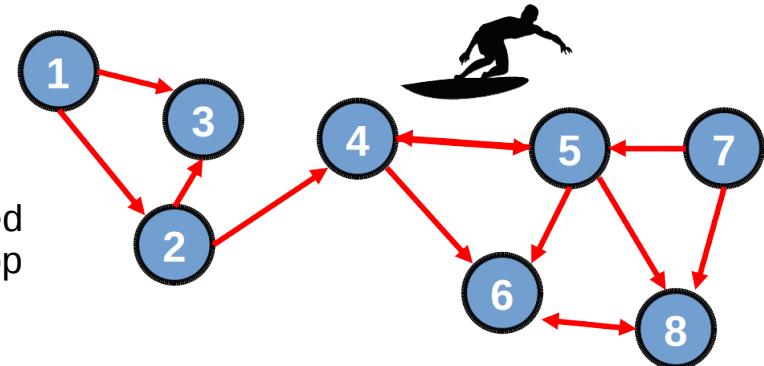
Stochastic matrix

$$\mathbf{S} = \begin{pmatrix} 0 & 0 & 1/8 & 0 & 0 & 0 & 0 & 0 \\ 1/2 & 0 & 1/8 & 0 & 0 & 0 & 0 & 0 \\ 1/2 & 1/2 & 1/8 & 0 & 0 & 0 & 0 & 0 \\ 0 & 1/2 & 1/8 & 0 & 1/3 & 0 & 0 & 0 \\ 0 & 0 & 1/8 & 1/2 & 0 & 0 & 1/2 & 0 \\ 0 & 0 & 1/8 & 1/2 & 1/3 & 0 & 0 & 1 \\ 0 & 0 & 1/8 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1/8 & 0 & 1/3 & 1 & 1/2 & 0 \end{pmatrix}$$

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Google matrix

$$G_{ij} = \alpha S_{ij} + (1 - \alpha)/N$$

avec $0.5 < \alpha < 1$

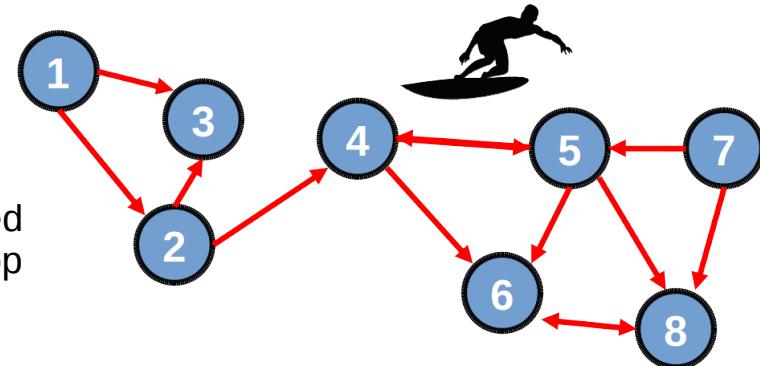
Perron-Frobenius operator

$$\mathbf{G} = \alpha = 0.8 \begin{pmatrix} 1/40 & 1/40 & 1/8 & 1/40 & 1/40 & 1/40 & 1/40 & 1/40 \\ 17/40 & 1/40 & 1/8 & 1/40 & 1/40 & 1/40 & 1/40 & 1/40 \\ 17/40 & 17/40 & 1/8 & 1/40 & 1/40 & 1/40 & 1/40 & 1/40 \\ 1/40 & 17/40 & 1/8 & 1/40 & 7/24 & 1/40 & 1/40 & 1/40 \\ 1/40 & 1/40 & 1/8 & 17/40 & 1/40 & 1/40 & 17/40 & 1/40 \\ 1/40 & 1/40 & 1/8 & 17/40 & 7/24 & 1/40 & 1/40 & 33/40 \\ 1/40 & 1/40 & 1/8 & 1/40 & 1/40 & 1/40 & 1/40 & 1/40 \\ 1/40 & 1/40 & 1/8 & 1/40 & 7/24 & 33/40 & 17/40 & 1/40 \end{pmatrix}$$

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PageRank vector

$$\mathbf{P} = \lim_{n \rightarrow \infty} \mathbf{P}^{(n)} = \lim_{n \rightarrow \infty} G^n \mathbf{P}^{(0)}$$

$P_i^{(n)}$ is the probability that random surfer arrives at node i at the n th step.

\mathbf{P} is the G matrix eigenvector associated with eigenvalue 1

$$\mathbf{P} = \mathbf{GP}$$

$$\mathbf{P} = \begin{pmatrix} 0.03109452568730597 \\ 0.04353233614756617 \\ 0.06094527086606558 \\ 0.06729412361797826 \\ 0.07044998599586171 \\ \textcolor{red}{0.35181679356094489} \\ 0.03109452568730597 \\ 0.34377243843697143 \end{pmatrix}$$

Distribution $P(K)$

where K is the rank index:

$$P(1) = \textcolor{red}{0.35181679356094489}$$

$$P(2) = 0.34377243843697143$$

$$P(3) = 0.07044998599586171$$

$$P(4) = 0.06729412361797826$$

$$P(5) = 0.06094527086606558$$

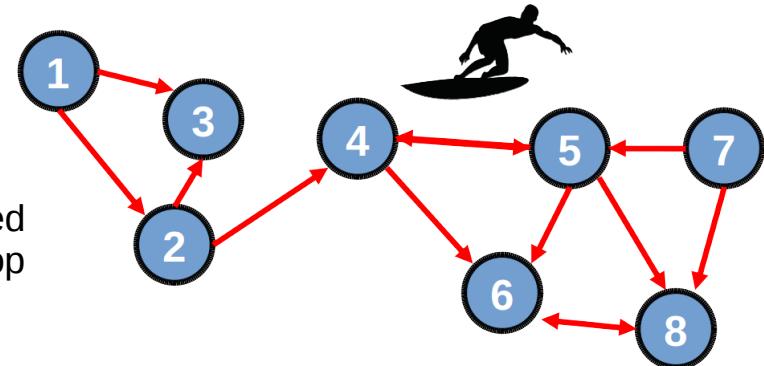
$$P(6) = 0.04353233614756617$$

$$P(7) = P(8) = 0.03109452568730597$$

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\mathbf{P} is the \mathbf{G} matrix eigenvector associated with eigenvalue 1

$$\mathbf{P} = \mathbf{G}\mathbf{P}$$

The most important node is the one with the highest probability.

“Recursive definition”: the more a node is pointed by important nodes, the more it is important.

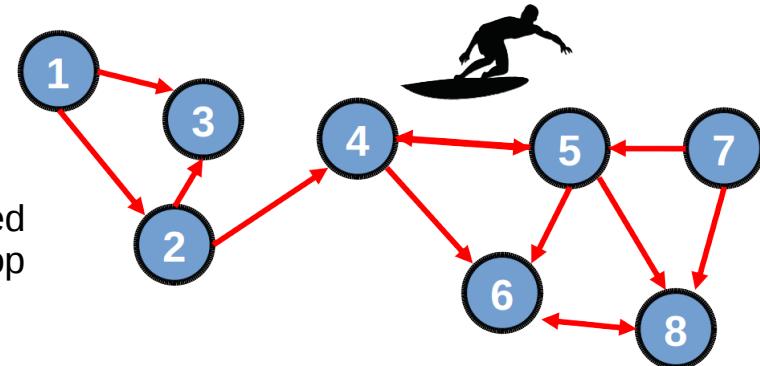
PageRank measures the influence of a node.

PageRank is (was?) at the heart of **Google** search engine (Brin, Page '98).

How Google works

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$$\text{CheiRank vector } \mathbf{P}^* = \mathbf{G}^* \mathbf{P}^*$$

Similar to PageRank of the inverted network. With inverted adjacency matrix elements $A_{ij}^* = A_{ji}$, it is possible to define the stochastic matrix elements $S_{ij}^* \neq S_{ji}$, and the Google matrix elements $G_{ij}^* \neq G_{ji}$ associated to the inverted network (Fogaras '03, Chepelianskii '10).

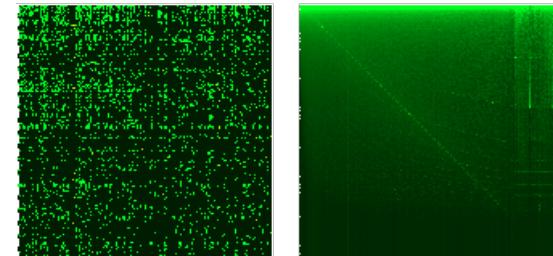
“Recursive definition”: the more a node pointed toward important nodes, the more it is important.

CheiRank measures the diffusion/the communication of a node.

Real directed complex networks

Properties of real networks (WWW, social networks, ...)

- “Small world” property: average distance between two nodes $\sim \log N$
- Scale-free property: distribution of the number of ingoing or outgoing links is $\rho(k) \sim k^{-\nu}$

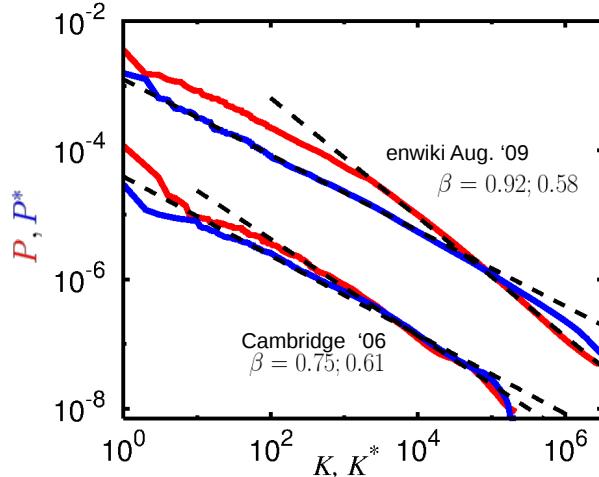


Google matrix G of the English Wikipedia network (Aug. '09)
N=3 282 257

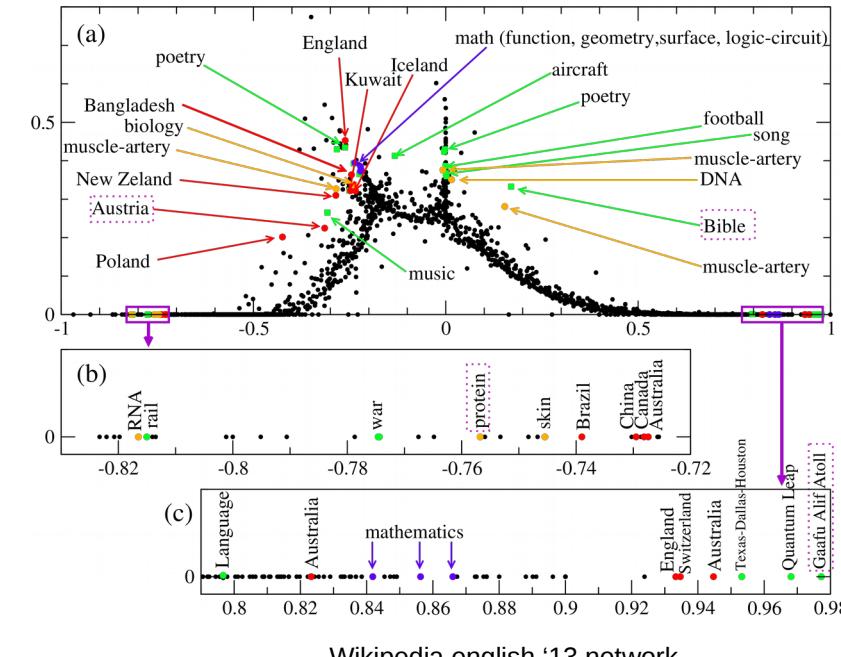
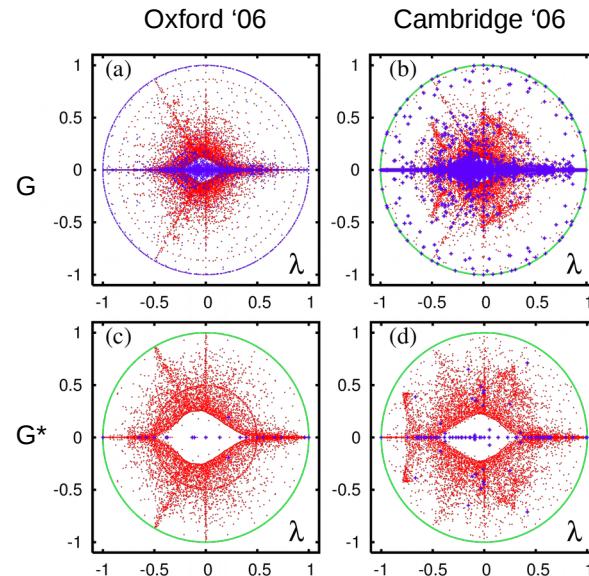
PageRank distribution properties

$$P(K) \sim 1/K^\beta \text{ with } \nu_{\text{in}} = 1 + 1/\beta$$

$$P^*(K^*) \sim 1/K^{*\beta} \text{ with } \nu_{\text{out}} = 1 + 1/\beta$$



Google matrix spectrum



Wikipedia english '13 network

Theory of real directed complex networks

Random Matrix Theory introduced by Wigner '67 describes universal spectral properties shared by complex nuclei/atoms/molecules and also mesoscopic and quantum chaos systems (Hermitean and unitary matrices statistical ensembles).

Challenge : A Random Matrix Theory for Markov chains and Google matrix ensembles is still lacking **We need more examples / more applications**

Figures from :
Ermann, Frahm, Shepelyansky
(2016), Scholarpedia,
11(11):30944

Ermann, Frahm, Shepelyansky
(2015), Rev. Mod. Phys. 87, 1261.

Big Data seen as directed networks

Non exhaustive list of applications

Data	Nodes	Links between nodes
WWW	Web pages	Hyperliens
Wikipedia	Wiki articles	Citations intra-wiki
Twitter / social networks	Members	Follow relations
World Trade (from WTO, UN, OECD, ...)	Goods x countries	Economical balance between countries
Omics	Proteins	Inhibition/activation
Linux	Kernel commands	Command succession
DNA	Pattern	Pattern successions
Brain activity	Neurons	Synaptic connections
Go game	Played patterns	Pattern sucessions

For a review, see Ermann, Frahm, Shepelyansky (2015), Rev. Mod. Phys. 87, 1261.

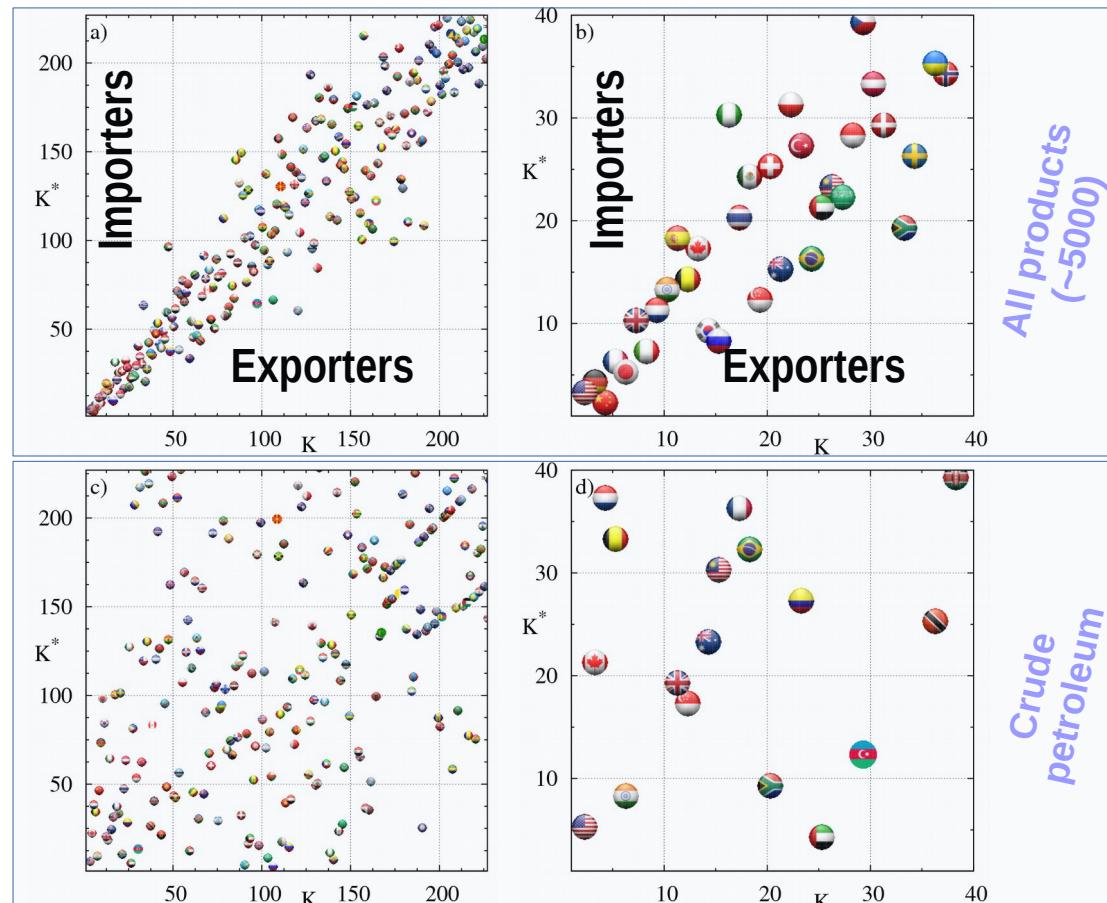
World Trade Google matrix

The analysis of World Trade Google matrix allows to treat every country, poor or rich, in **an equal footing**. Indeed, for a given country, imported quantities from or exported quantities toward another country are normalized by the total imported or exported (different point of view in comparison with usual import-export classification).

PageRank naturally characterizes the capacity of a country to **import**.

CheiRank naturally characterizes the capacity of a country to **export**.

75% overlap between **top 20** countries in K-K* plane and G20 members

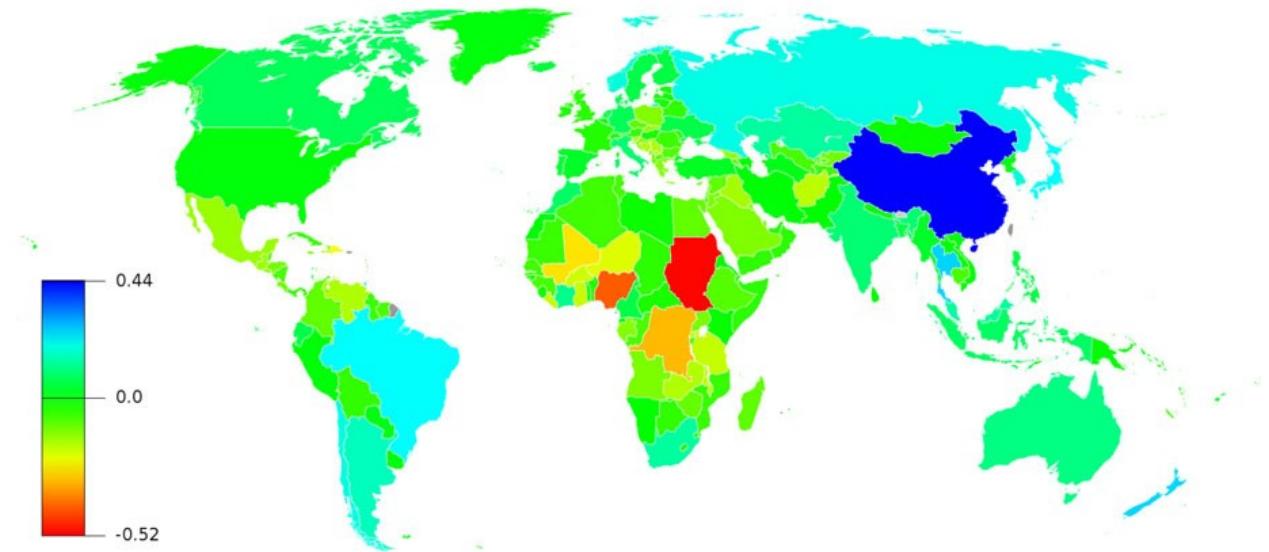


Data from UN-COMTRADE
227 countries
~5000 products

Ermann, Shepelyansky '11

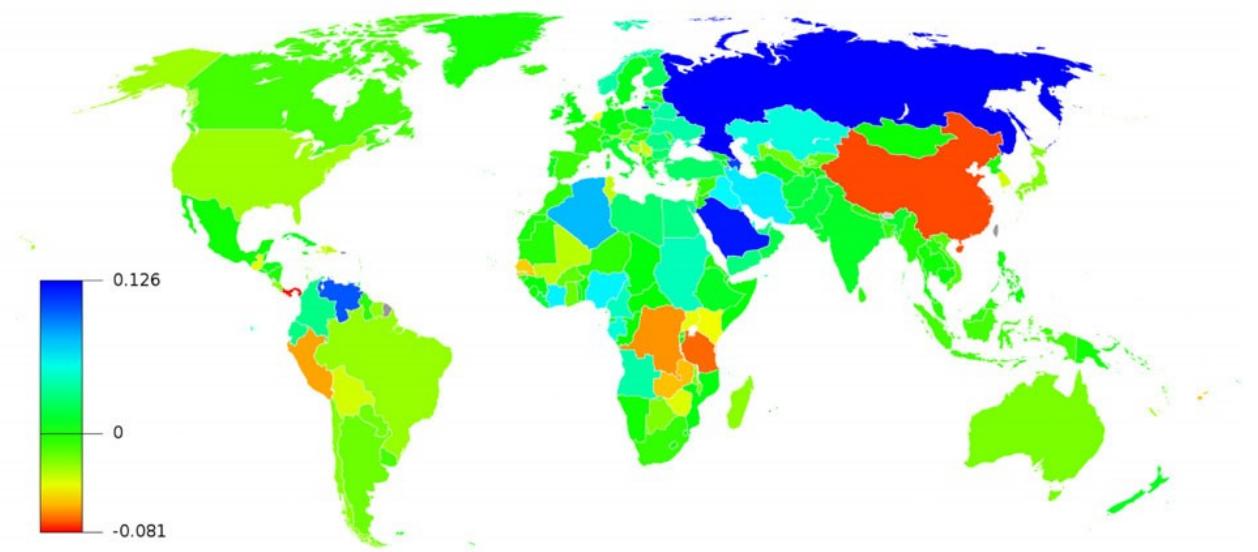
World Trade Google matrix

PageRank-CheiRank balance



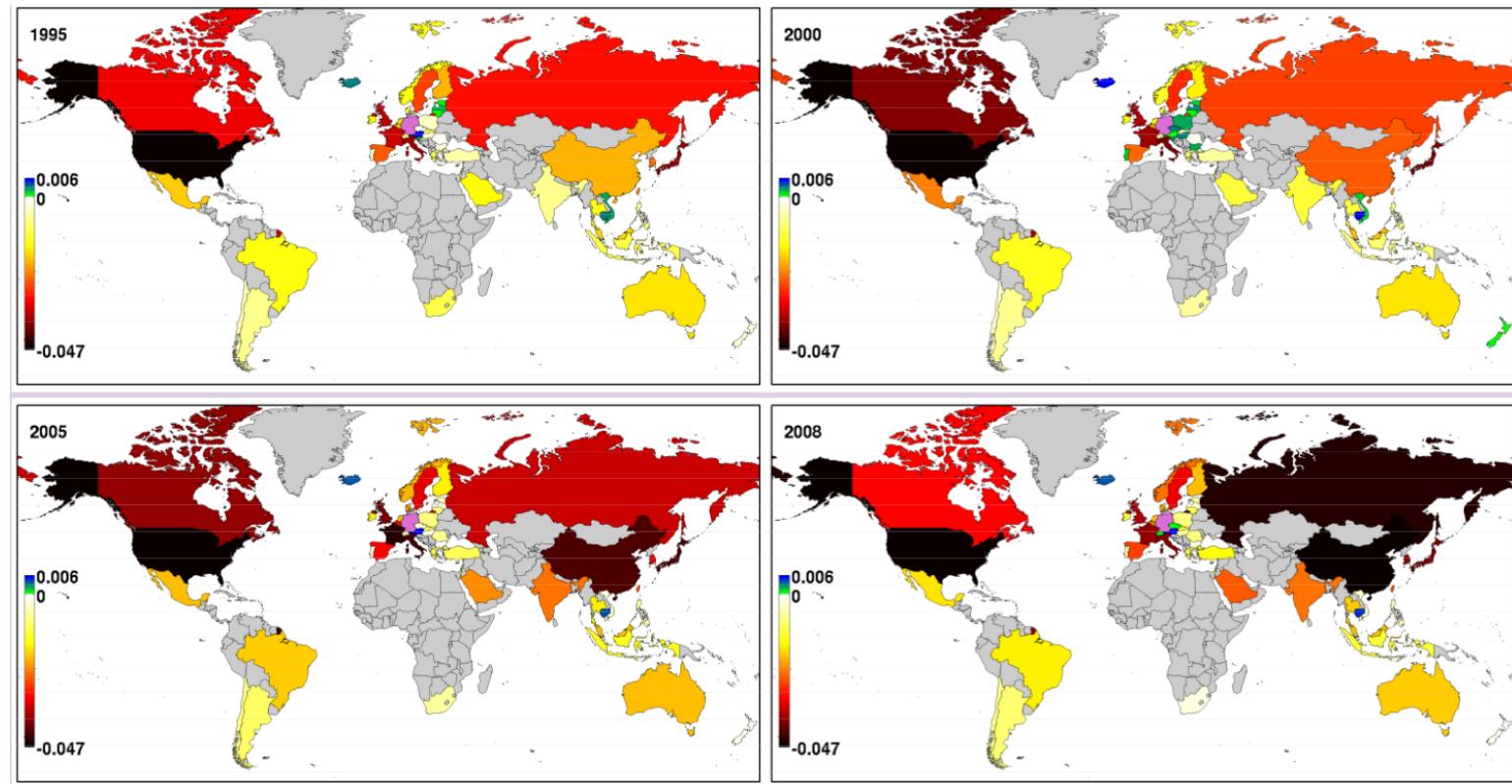
Sensitivity of the PageRank-CheiRank balance to the increase petroleum cost

Data from UN '14



World Trade Google matrix

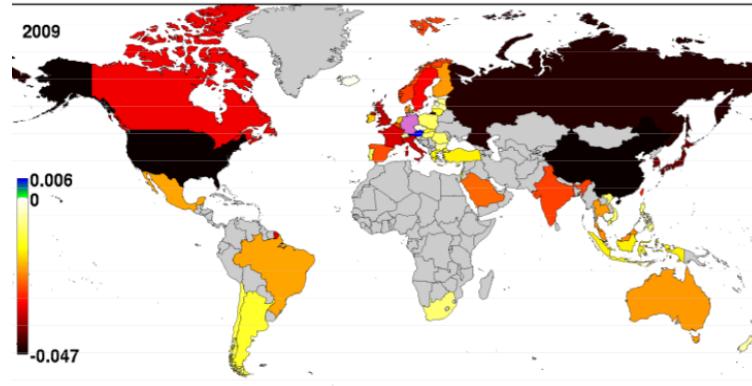
Sensitivity over the years of the PageRank-CheiRank balance to the increase of labor cost in Germany



Data from WTO
58 countries
37 activity sectors

Collaboration with H. Escaith from WTO
Geneva

Kandiah, Escaith, Shepelyansky '15



Study of crisis
Recommendations
Risks

Highlight of some results from ApliGoogle project

WRWU: Wikipedia Ranking of World Universities

24 Wikipedia language editions
covering 59% of world population
and 68% total Wikipages

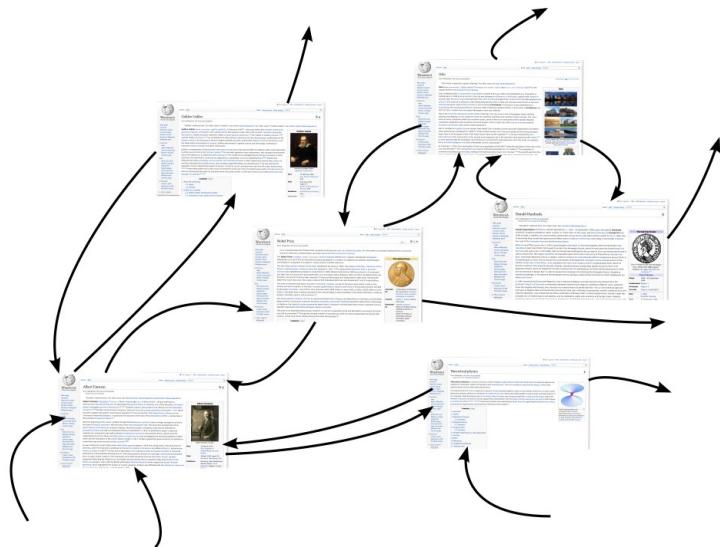
Edition	Language	N	Edition	Language	N
EN	English	4 212 493	VI	Vietnamese	594 089
DE	German	1 532 978	FA	Persian	295 696
FR	French	1 352 825	HU	Hungarian	235 212
NL	Dutch	1 144 615	KO	Korean	231 959
IT	Italian	1 017 953	TR	Turkish	206 311
ES	Spanish	974 025	AR	Arabic	203 328
RU	Russian	966 284	MS	Malaysian	180 886
PL	Polish	949 153	DA	Danish	175 228
JA	Japanese	852 087	HE	Hebrew	144 959
SV	Swedish	780 872	HI	Hindi	96 869
PT	Portuguese	758 227	EL	Greek	82 563
ZH	Chinese	663 485	TH	Thai	78 953

About 17M wikipages considered
(March '13)



WIKIPEDIA
The Free Encyclopedia

Each Wikipedia edition is treated as
a complex network



All these rankings are composite:



•
•
•

About **20 different** global university
rankings are listed in the Wikipedia
page "College and university rankings"



+ ...

Composite score



Also, universities are preselected

These rankings have
an impact on scientific
and educational policies
of governments

Is
there
an universal
ranking without
a priori criteria and
without cultural bias ?

WRWU: Wikipedia Ranking of World Universities

1024 ranked Universities

Wikipedia PageRanking of World Universities WRWU

- 1st University of Cambridge
- 2nd University of Oxford
- 3rd Harvard University
- 4th Columbia University
- 5th Princeton University
- 6th MIT
- 7th University of Chicago
- 8th Stanford University
- 9th Yale University
- 10th University of California, Berkeley

Oxbridge at the top of WRWU
followed by **US major universities**

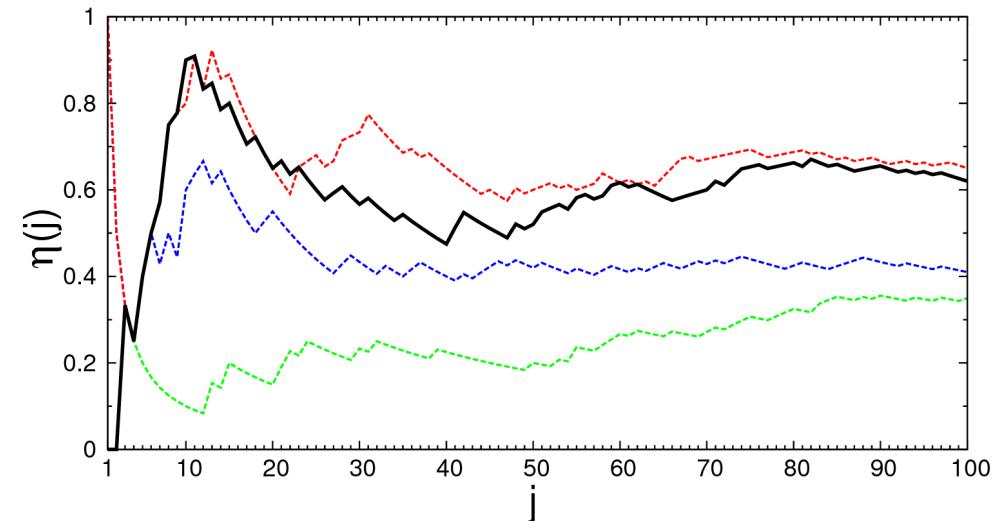


Academic Ranking of World Universities ARWU ("Shanghai ranking" 2013)

- 1st Harvard University (-2)
- 2nd Stanford University (-6)
- 3rd University of California, Berkeley (-7)
- 4th MIT (-2)
- 5th University of Cambridge (+4)
- 6th California Institute of Technology (-22)
- 7th Princeton University (+2)
- 8th Columbia University (+4)
- 9th University of Chicago (+2)
- 10th University of Oxford (+8)

90% overlap
between top 10s
WRWU and ARWU

60% overlap
between top 100s
WRWU and ARWU



Definitely, as ARWU, WRWU measures academic excellence but not only ...

J. Lages, A. Patt, D. L. Shepelyansky, The European Physical Journal B (2016) 89: 69

WRWU: Wikipedia Ranking of World Universities

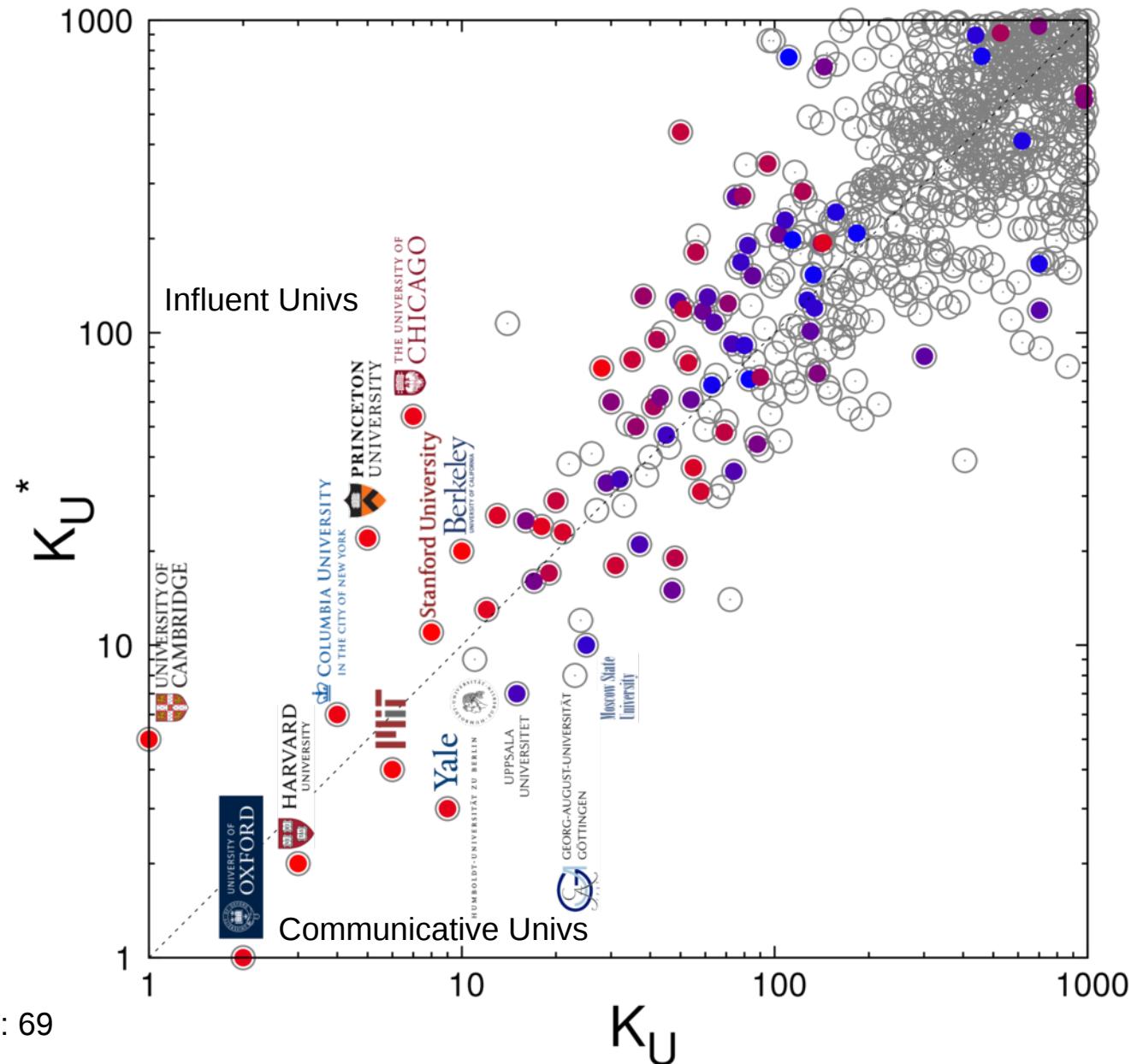
... WRWU measures also historical, societal and regional importance of universities.

WRWU is free from any cultural preferences since :

- it takes into account many cultural point of view as we use encyclopaedic knowledge contained in 24 Wikipedia language editions (17 millions wiki articles)
- these points of view are treated on equal footing with the same statistical analysis (PageRank, CheiRank, ...)

WRWU can be considered as **complementary** to already existing rankings such as ARWU (Shanghai), THE, ..., but in fact it **encodes already all existing rankings** since Wikipedia contains information on it.

Universal ranking ?



J. Lages, A. Patt, D. L. Shepelyansky
The European Physical Journal B (2016) 89: 69

WRWU: Wikipedia Ranking of World Universities

Web page of WRWU with detailed data (ranking by country, by foundation century, ...)
Is your Univ. well ranked ? Check at : <http://perso.utinam.cnrs.fr/~lages/datasets/WRWU/>

In the media (100 press articles in 22 countries) : <http://perso.utinam.cnrs.fr/~lages/datasets/WRWU/press/Press.html>



Reduced Google matrix

Consider a network with $N \gg 1$ nodes.

Consider a sub-network (a community) of $N_r \ll N$ nodes. Google matrix of the N size network and the associated PageRank vector can be written

$$\mathbf{G} = \begin{pmatrix} \mathbf{G}_{rr} & \mathbf{G}_{rs} \\ \mathbf{G}_{sr} & \mathbf{G}_{ss} \end{pmatrix}, \quad \mathbf{P} = \begin{pmatrix} \mathbf{P}_r \\ \mathbf{P}_s \end{pmatrix}$$

$$\mathbf{GP} = \mathbf{P}$$

We define the reduced Google matrix \mathbf{G}_R associated to the size N_r community such as

$$\mathbf{G}_R \mathbf{P}_r = \mathbf{P}_r$$

The reduced Google matrix can be written

$$\mathbf{G}_R = \boxed{\mathbf{G}_{rr}} + \boxed{\mathbf{G}_{rs} (1 - \mathbf{G}_{ss})^{-1} \mathbf{G}_{sr}}$$

↓ ↓
Contribution
from direct
links Contribution from
indirect links
(scattering term)

$$(1 - \mathbf{G}_{ss})^{-1} = \sum_{l=0}^{\infty} \mathbf{G}_{ss}^l$$

Very slow convergence since the eigenvalue λ_c of $\mathbf{G}_{ss} \sim \mathbf{G}$ is very close to 1.

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$$\mathbf{G}_R \mathbf{P}_r = \mathbf{P}_r$$

The reduced Google matrix can be written

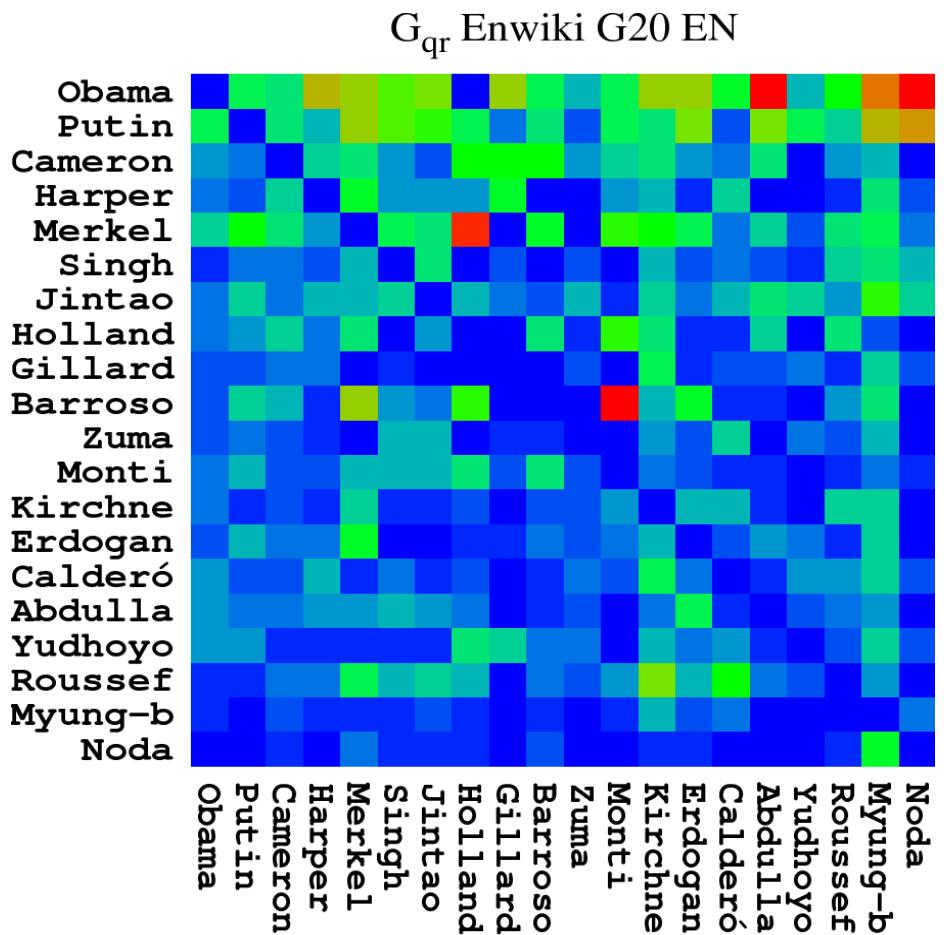
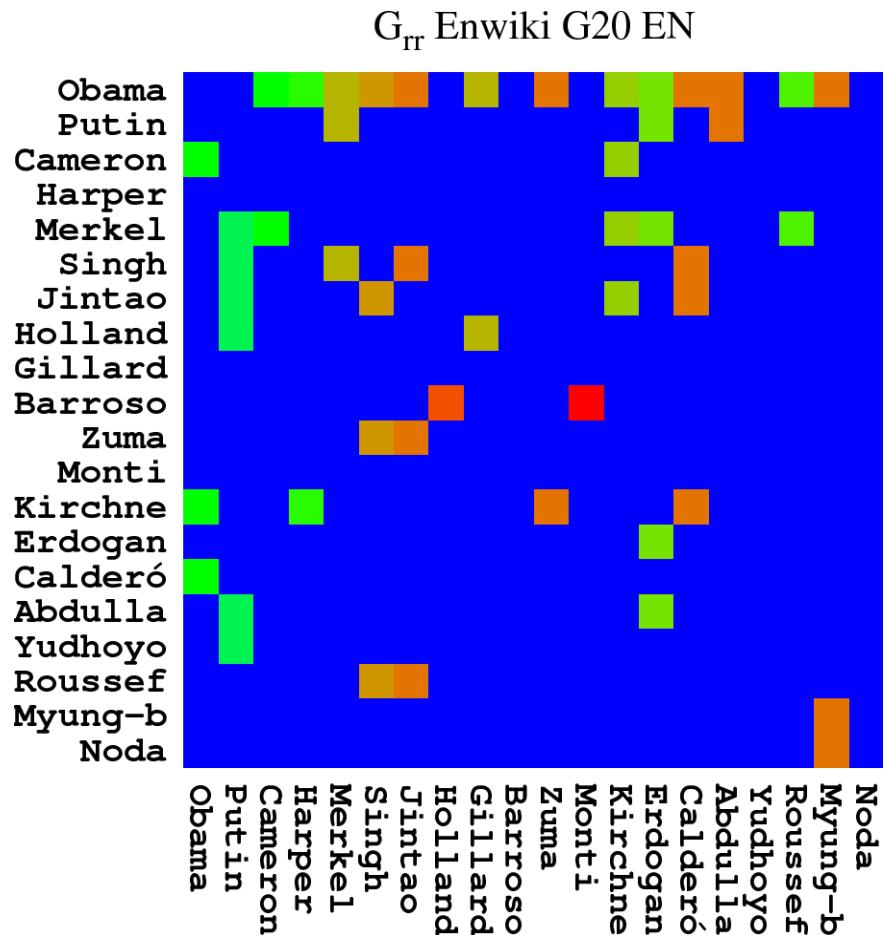
$$\mathbf{G}_R = \mathbf{G}_{rr} + \mathbf{G}_{pr} + \mathbf{G}_{qr}$$

Diagram illustrating the components of the reduced Google matrix \mathbf{G}_R :

- \mathbf{G}_{rr} (blue box) is labeled "Contribution from direct links" (blue text) with a blue arrow pointing down.
- \mathbf{G}_{pr} (green box) is labeled "Contribution from hidden links" (red text) with a red arrow pointing down.
- \mathbf{G}_{qr} (pink box) is labeled "Contribution from « PageRank »" (green text) with a green arrow pointing down.

Wikipedia mining of hidden links between political leaders

2013 Wikipedia edition



$$G_R = G_{rr} + G_{pr} + G_{qr}$$

direct links hidden links

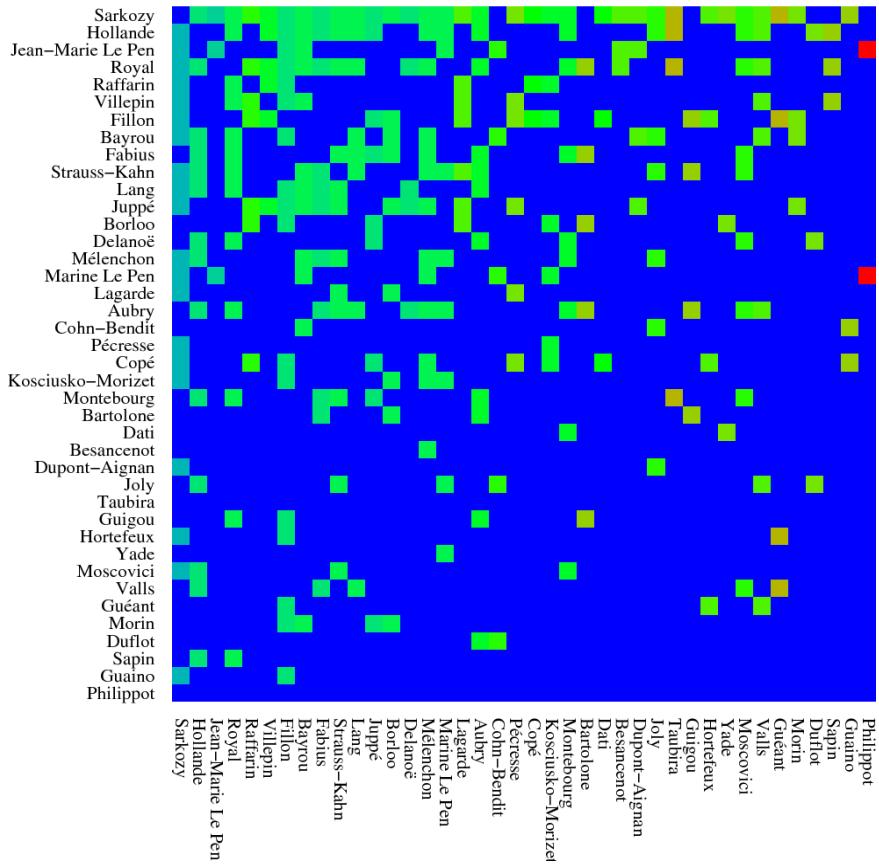
Frahm, Jaffrèses-Runser, Shepelyansky, Eur. Phys. J. B (2016) 89: 269

Colloque de restitution du Défi MASTODONS CNRS 2016 – jeudi 9 février 2017

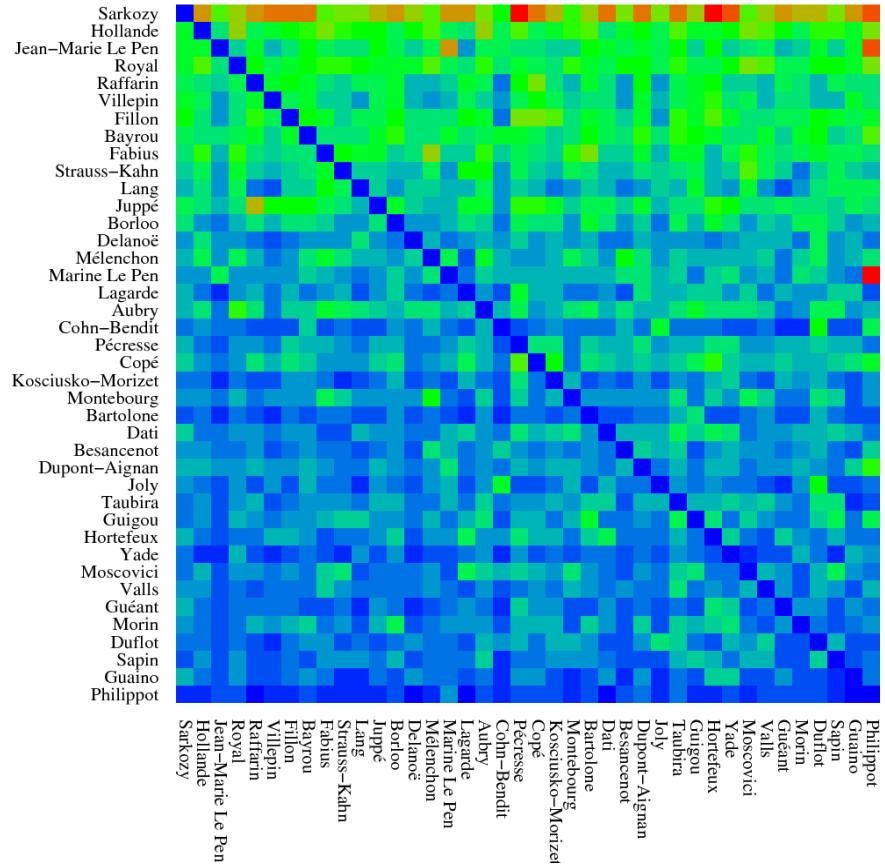
Wikipedia mining of hidden links between political leaders

2013 Wikipedia edition

G_{rr} Frwiki Politicians FR



G_{qr} Frwiki Politicians FR



$$G_R = G_{rr} + G_{pr} + G_{qr}$$

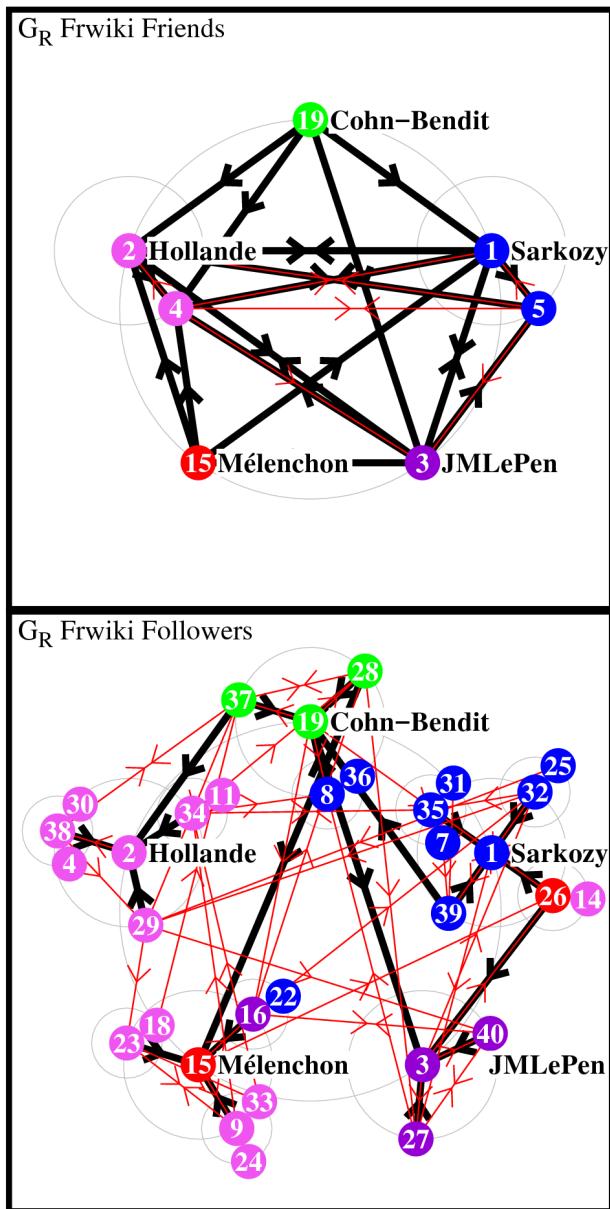
direct links hidden links

Frahm, Jaffrès-Runser, Shepelyansky, Eur. Phys. J. B (2016) 89: 269

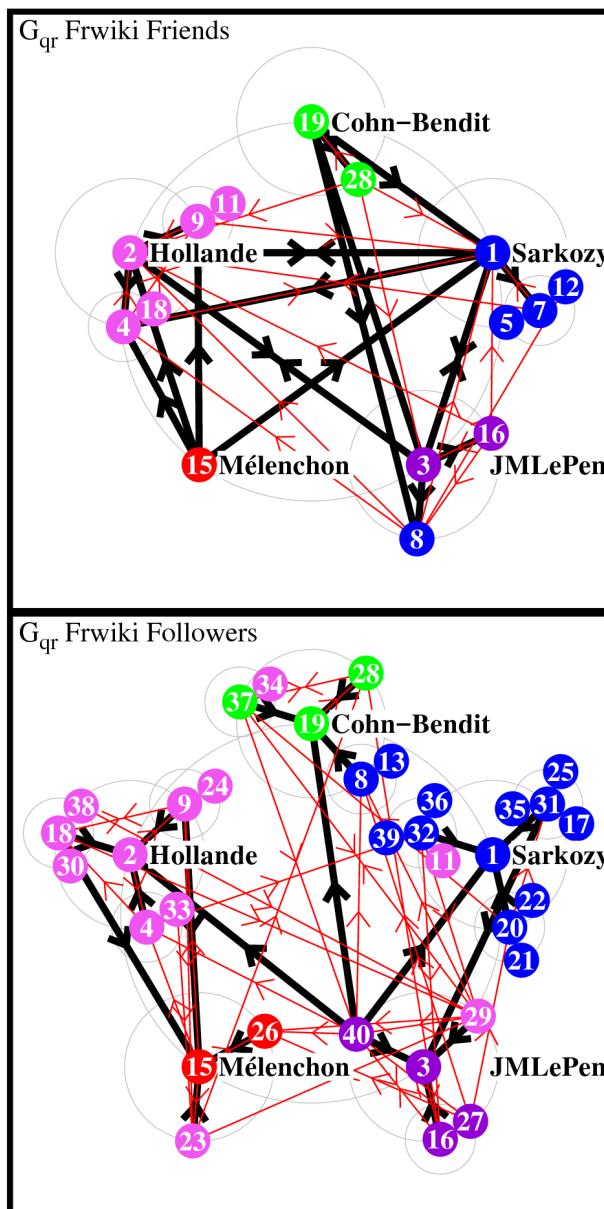
Colloque de restitution du Défi MASTODONS CNRS 2016 – jeudi 9 février 2017

Wikipedia mining of hidden links between political leaders

Circles of influence



2013 Wikipedia edition



Names (FR)	K
Nicolas Sarkozy CB	1
François Hollande CM	2
Jean-Marie Le Pen CV	3
Ségolène Royal CM	4
Jean-Pierre Raffarin CB	5
Dominique de Villepin CB	6
François Fillon CB	7
François Bayrou CB	8
Laurent Fabius CM	9
Dominique Strauss-Kahn CM	10
Jack Lang CM	11
Alain Juppé CB	12
Jean-Louis Borloo CB	13
Bertrand Delanoë CM	14
Jean-Luc Mélenchon CR	15
Marine Le Pen CV	16
Christine Lagarde CB	17
Martine Aubry CM	18
Daniel Cohn-Bendit CG	19
Valérie Péresse CB	20
Jean-François Copé CB	21
Nathalie Kosciusko-Morizet CB	22
Arnaud Montebourg CM	23
Claude Bartolone CM	24
Rachida Dati CB	25
Olivier Besancenot CR	26
Nicolas Dupont-Aignan CV	27
Eva Joly CG	28
Christiane Taubira CM	29
Élisabeth Guigou CM	30
Brice Hortefeux CB	31
Rama Yade CB	32
Pierre Moscovici CM	33
Manuel Valls CM	34
Claude Guéant CB	35
Hervé Morin CB	36
Cécile Duflot CG	37
Michel Sapin CM	38
Henri Guaino CB	39
Florian Philippot CV	40

$$G_R = G_{rr} + G_{pr} + G_{qr}$$

direct links

hidden links

Frahm, Jaffrès-Runser, Shepelyansky, Eur. Phys. J. B (2016) 89: 269

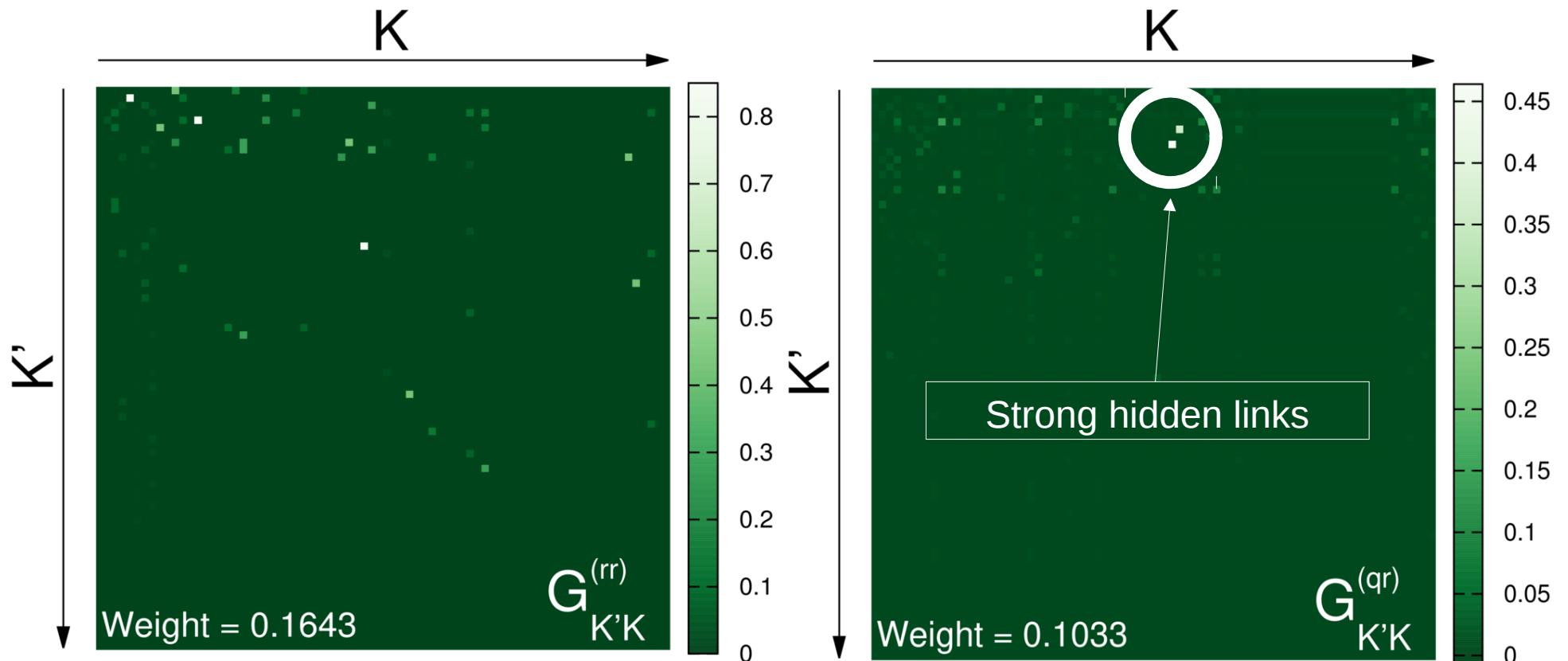
Colloque de restitution du Défi MASTODONS CNRS 2016 – jeudi 9 février 2017

Google matrix analysis of causal cancer protein networks

Hidden interactions between proteins

Global network (signaling network SIGNOR) 2432 proteins (nodes)

Example of a sub-network of 76 proteins (direct transcriptional targets of E2F1 protein)



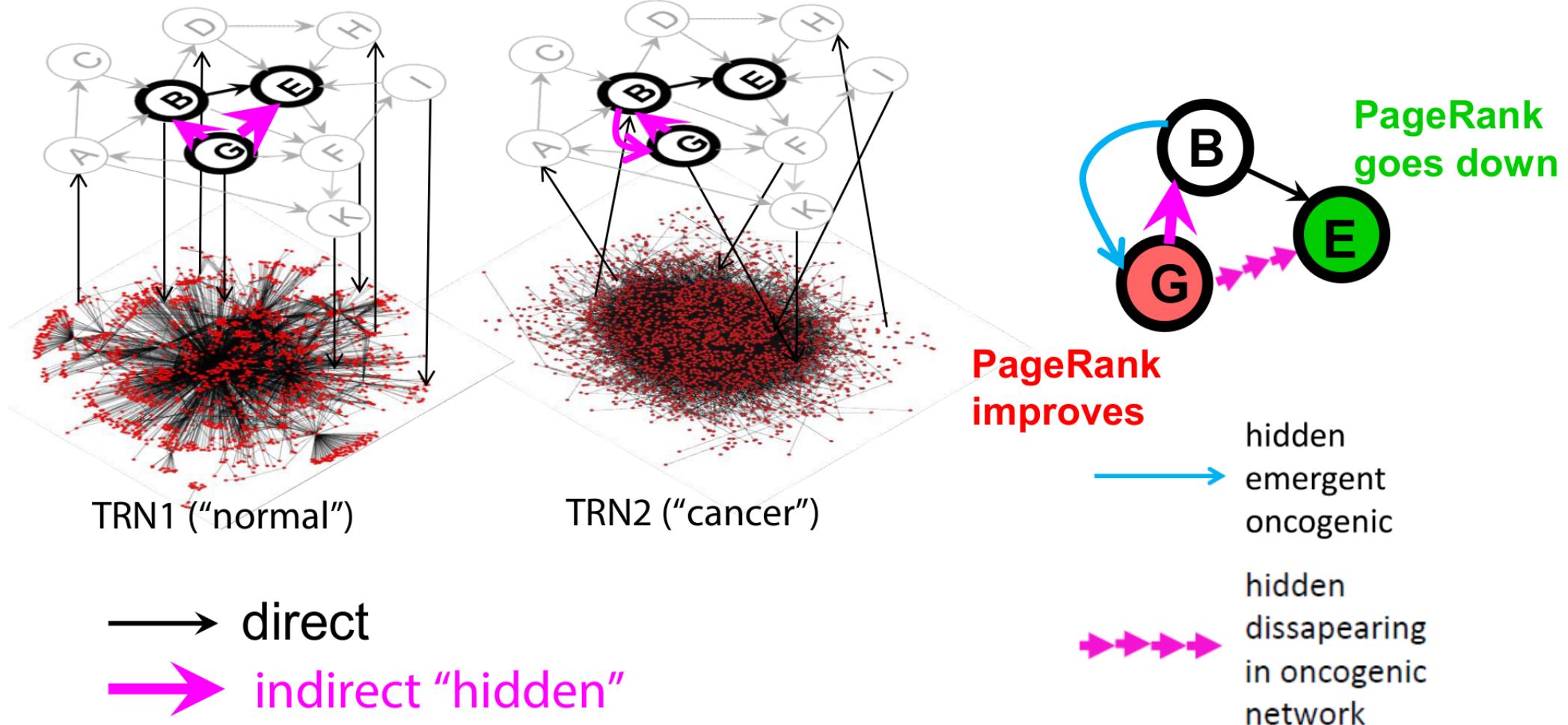
$$G_R = G_{rr} + G_{pr} + G_{qr}$$

direct links hidden links

Lages, Shepelyansky, Zinovyev, bioRxiv 096362, submitted to eLife

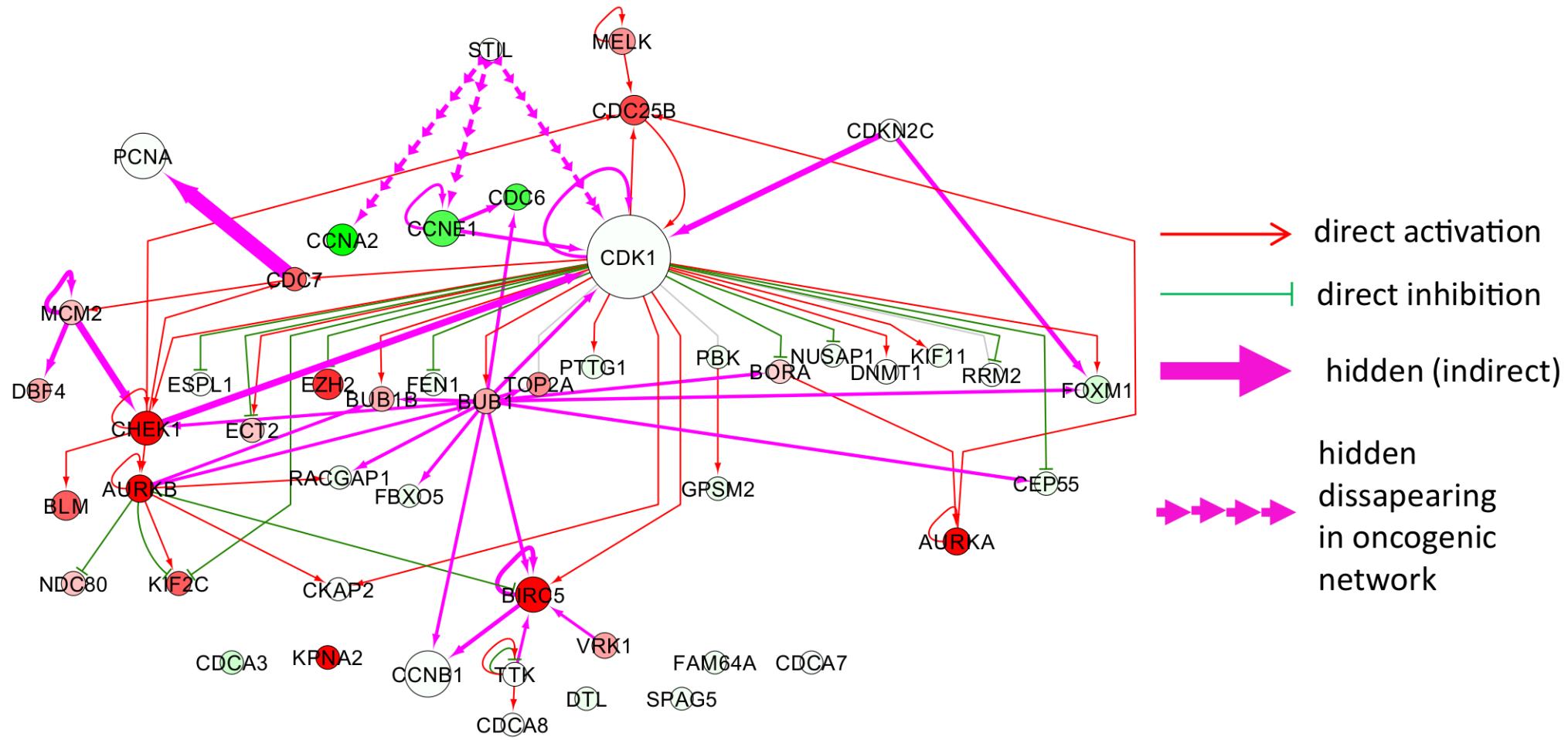
Google matrix analysis of causal cancer protein networks

General scheme



Lages, Shepelyansky, Zinovyev, bioRxiv 096362, submitted to eLife

Google matrix analysis of causal cancer protein networks



Network of proteins shown to be related to cell proliferation by transcriptomic data analysis. The meaning of the node and edge colors is the same as in Figure 6 besides those regulations which disappear in "cancer" network compared to "normal" network (shown by interrupted line arrows).

Lages, Shepelyansky, Zinov'yev, bioRxiv 096362, submitted to eLife

Planned further works

Planned further works

- **Global multiproduct world trade network**
Merging UN, WTO and OECD data to construct a global network of about 2 million nodes.
Analysis of global world trade along decades.
Use of reduced Google matrix to find hidden links between activity sectors or products.
- **Bitcoin transactions network**
Currently about 10 millions transaction per month / 10 billion US dollars volume.
- **Global multilingual Wikipedia network**
Build a global Wikipedia network (size about 20 million nodes/articles) using the links between articles from different language editions.
Use of reduced Google matrix to find hidden links between concepts (many possible directions of investigation)
- **Mobile network / Social network**
With data collected from a bunch of mobile, construct a network of applications/instructions.
- **Googlomics : application of Google matrix to mulfunctionnal network of omics (proteins, genes, ...)**



Bitcoin transactions network density in PageRank-CheiRank plane for all period from creation in 2009 till April 2013 (about 2 million users, the number of transactions is about 20 millions) [preliminary result]

Thank You !