



Proposal of experimental realization
of 3D Anderson transition with kicked cold atoms
by D.L.Shepelyansky
(2 letters to J.C.Garreau at 29 July and 3 Oct 2005).

Email 1

-----Message d'origine-----

De : dima [mailto:dima@irsamc.ups-tlse.fr]

Envoye: vendredi 29 juillet 2005 13:39

A : Jean-Claude Garreau

Objet : Re: Preprint

Dear Professor Garreau,

thank for the preprint of your nice experiment.

I would like to ask the following:

you have now about 100kicks

and it seems to me that with your equipment

it is possible to see experimentally

3d Anderson transition with cold atoms

for the first time

(I tried to convince Raizen to do this

in 1994 but his claim was that he has not enough kicks).

To have this transition

you should replace

$[1-\epsilon\cos(\omega t)]$

by

$[1-\epsilon\cos(\omega t)\cos(\omega_1 t)]$

and take $\omega/2\pi$ and $\omega_1/2\pi$

as two irrational numbers. □

Numerical data of Ref.1 (pdf attached)

shows that the Anderson transition

takes place around $K/\hbar v = 1.8$

for $\epsilon=0.75$ (see Fig.1 there).

This 3d Anderson transition

had been also discussed in Refs.2-4.

(pdfs are available from my publication list

on my web page).



I will be glad to give more information.

With best regards,

Dima Shepelyansky

<http://www.lpt.irsamc.ups-tlse.fr/~dima>

Refs:

Ref.1

76. F.Borgonovi, D.L.Shepelyansky, "Two interacting particles in an effective 2-3-d random potential", J. de Physique I France v.6 (1996) p.287-299 (cond-mat/9507107)

□

Ref.2

37. G.Casati, I.Guarneri, D.L.Shepelyansky, "Anderson Transition in a One-Dimensional System with Three Incommensurate Frequencies", Phys. Rev. Lett. v.62, p.345-348 (1989)

Ref.3

86. F.Borgonovi and D.L.Shepelyansky, "Particle propagation in a random and quasi-periodic potential", Physica D, v.109 (1997) p.24-31 (cond-mat/9610137)

Ref.4

141. A.A.Pomeransky and D.L.Shepelyansky, "Quantum computation of the Anderson transition in the presence of imperfections", Phys. Rev. A v.69 (2004) p.014302 (quant-ph/0306203)



Email 2

Date: Mon, 3 Oct 2005 21:06:49 +0200 (CEST)

From: dima <dima@irsamc.ups-tlse.fr>

To: Jean-Claude Garreau <jean-claude.garreau@univ-lille1.fr>

Subject: Re: RE : RE : Preprint

Parts/Attachments:

1	Shown	46 lines	Text
2	OK	39 KB	Application, "diff.ps"
3	OK	46 KB	Application, "prob.ps"
4	OK	42 KB	Application, "prob0.ps"

Bonjour Jean-Claude,

attached are figs in postscript
for kicked rotator at $k=1; 1.5; 2.0; 2.2$
and $\hbar=2$; thus chaos parameter
is $K=k \hbar$ that corresponds to chaotic regime.

Fig diff.ps shows second moment of
distribution during 200 kicks.
It clearly shows that $k=1; 1.5$ are
localized while $k=2.0$ is delocalised so
thus the Anderson transition
is somewhere in between.

Fig prob.ps shows decimal log
of level probability W_p vs level number
for the value of k given above
(the change from parabolic
to linear cusp shape also shows
the transition around 1.8).

fig prob0.ps
shows probability P_0 at initial zero $n=0$ state
as a function of time for the cases of fig diff.ps.
Here fluctuations are too strong to see the existence
of transition. Even if in experiment you will
have very good averaging over many
quasi-momentum states I doubt that
 P_0 is a good characteristic,
indeed in 1d diffusion
the probability at zero drops as $1/\sqrt{t}$
that is too slow for a given time interval.



I think the only way to detect the transition is to measure λ_p as it had been done by Raisen. You may show λ_p at different moments of time showing frozen and diffusive spreading.

in cases above the kick amplitude is
 $k(t) = k(1 + 0.75 \cos \omega t \cos(\omega_1 t))$
with $\omega = 2\pi/1.3247$; $\omega_1 = \omega/1.3247$.
runs are for quasimomentum=0

best regards,
Dima

====NOTE====>these figs are at the end of file in this order:

[Part 2, "diff.ps" Application/POSTSCRIPT 52KB.] ==>4 pages
[Not Shown. Use the "V" command to view or save this part.]

[Part 3, "prob.ps" Application/POSTSCRIPT 62KB.] ==> next 4 pages
[Not Shown. Use the "V" command to view or save this part.]

[Part 4, "prob0.ps" Application/POSTSCRIPT 57KB.] ==> next 4 pages
[Not Shown. Use the "V" command to view or save this part.]

figs files are given below:

diff.pdf (4 pages); prob.pdf (4 pages); prob0.pdf (4 pages)























